

## QUANTITATIVE TECHNIQUES II

### Class Requirements

There will be **5** problem sets. These will be graded coarsely (P+, P, P-). It is **strongly** recommended that you attempt the problem sets yourself. You may discuss difficulties with your classmates, the TA, myself (in that order) if you are stuck.

Further, there will be 2 in-class midterms and a final exam (all are close book). The 2<sup>nd</sup> midterm will only cover material since the first midterm. The final exam is cumulative. I will make sample exams available about a week before the actual exam.

Grades for the class will be based on:

1. Midterm (20% each) (In class, on September 25, October 30)
2. Problem sets (10%)
3. Final Exam (50%) (In class, December 2)

### Readings

There is no required textbook for the class, but you are encouraged to have one of the following real analysis textbooks:

- A. Kolmogorov, and S. Fomin, *Introductory Real Analysis*, Dover Publications, 1975.
- C. Pugh, *Real Mathematical Analysis*, Springer, 2001
- W. Rudin, *Principles of Mathematical Analysis*, McGraw-Hill, 1976.

You might find the following books are also useful for certain topics:

- D. Corbae, M. Stinchcombe, and J. Zeman, *An Introduction to Mathematical Analysis for Economic Theory and Econometrics*, Princeton Univ. Press, Princeton, 2009.
- E. Ok, *Real Analysis with Economic Applications*, Princeton Univ. Press, 2007.
- N. Stokey, and R. Lucas, *Recursive Methods in Economic Dynamics*, Harvard Univ. Press, Cambridge, Massachusetts, 1989.
- R. Sundaram, *A First Course in Optimization Theory*, Cambridge Univ. Press, Cambridge, 1996.
- R. Vohra, *Advanced Mathematical Economics*, Routledge, 2005.

In addition, the previous instructor of this course, Peter Norman, has an excellent lecture notes on his website.

### Class Logistics

The class meets on Tuesday and Thursday 12:30-1:45 pm at Gardner Hall 307. You are expected to attend all classes. There is no lecture in the following date: Oct. 16<sup>th</sup>, and Nov. 27<sup>th</sup>.

Assignments will be posted on Sakai. There will be weekly review sessions.  
Assignments are due in review session at the beginning of the lecture on the due date.

### Contacting Us

My e-mail is [lifei@email.unc.edu](mailto:lifei@email.unc.edu). My office is Gardner 300B. My office hour is TR 4:45-5:15pm. Your TA is Sam Flanders. His email is [samf1986@gmail.com](mailto:samf1986@gmail.com).

### Tentative Agenda

1. Set Theory and Functions (~1-2 weeks)
  - a. Operations on Sets
  - b. Functions and Mappings
  - c. Finite and Infinite Sets
  - d. Countability
2. Topology in Metric Space (~2-3 weeks)
  - a. Open and Closed Sets
  - b. Sequences, Limits and Convergence
  - c. Continuity
  - d. Compactness and Weierstrass Theorem
  - e. Completeness
  - f. Connectness and Intermediate Value Theorem
3. Function Space (~1 weeks)
  - a. Uniform Convergence in  $C^0[a,b]$
  - b. Compactness and Equicontinuity in  $C^0[a,b]$
  - c. Uniform Approximation in  $C^0[a,b]$
4. Contraction Mapping Theorem and Its Applications (~1-2 weeks)
  - a. Contraction Mapping Theorem
  - b. Implicit Function Theorem
  - c. Applications
5. Linear Space (~2 weeks)
  - a. Definition and Properties of Linear Space
  - b. Half Space, Hyperplane
  - c. Hyperplane Separation (Supporting) Theorem
  - d. Farkas Lemma
  - e. Applications
6. Optimization in  $\mathbb{R}^n$  (~2-3 week)
  - a. Problem and Existence
  - b. Linear Programming
  - c. Convex, Concave, and Quasi-Concave Functions
  - d. Convex Programming
  - e. Maximum Theorem
  - f. Envelop Theorem
7. Sup-modularity (optional)